



Rotating magnetic quadrupole RMF current drive for FRCs

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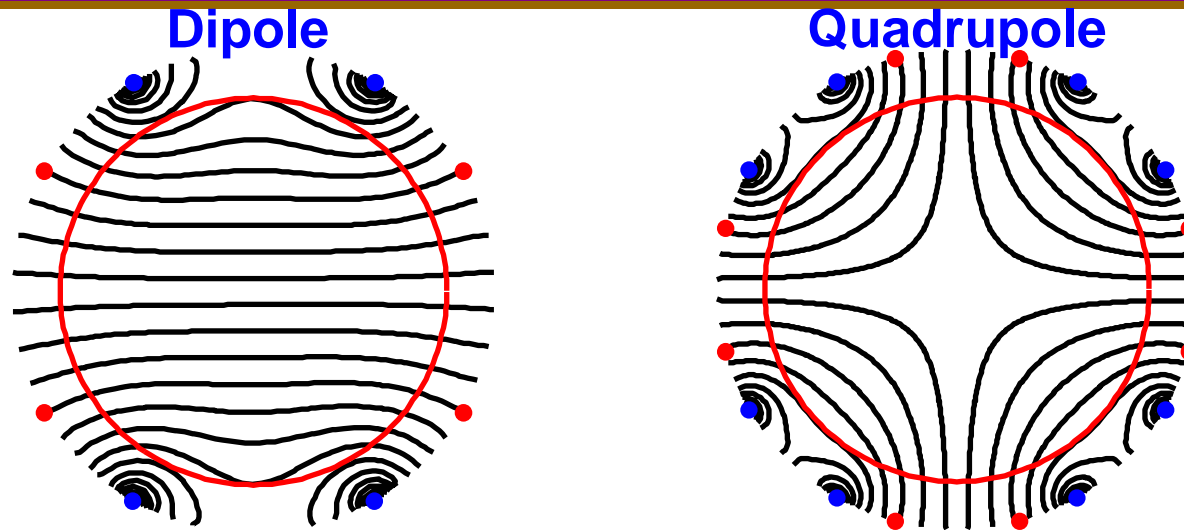
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Outline



- Introduction:
 - What is Quadrupole RMF current drive?
- Why attempt quadrupole RMF current drive?
- Numerical Predictions
- Experimental observations
 - Comparable drive capability
 - More prone to $n=2$ instabilities
 - Large internal oscillations for some parameters
- Summary

Quadrupole vs. dipole



For a quadrupole:

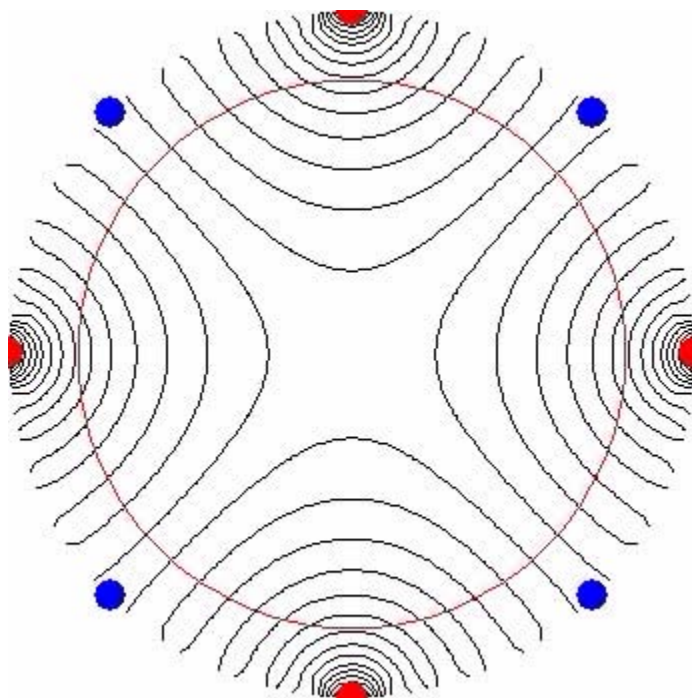
$$B_r = -\frac{4\mu_o I}{\pi} \sum_{n=2,6,10,\dots} \left\{ \frac{\cos(n\alpha)}{R_c} \left(\frac{r}{R_c} \right)^{n-1} \sin \left(n\theta + (-1)^{\frac{n+2}{4}} \omega t \right) \right\}$$

- Quadrupole field does not penetrate to $r = 0$ ($B_r \propto r$).
 - Not a problem since RMF is usually confined to the FRC edge.
- Coil separation of $\frac{1}{2}$ angle $\alpha = \pi/12 \rightarrow n=6$ mode is zeroed (optimum angle)
- The rotation rate of the RMF field, $\omega_{rot} \propto \frac{1}{2}\omega_{rmf}$

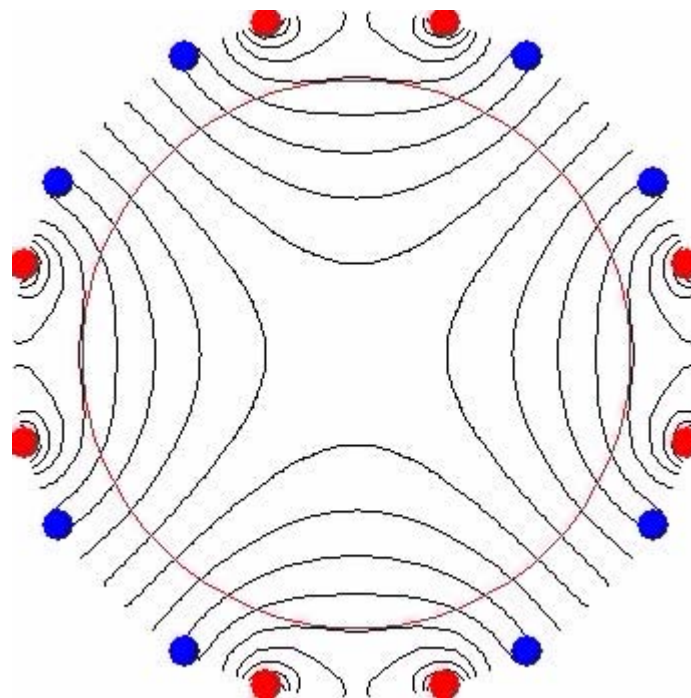
Vacuum Quadrupole Field



Simple quadrupole coil set



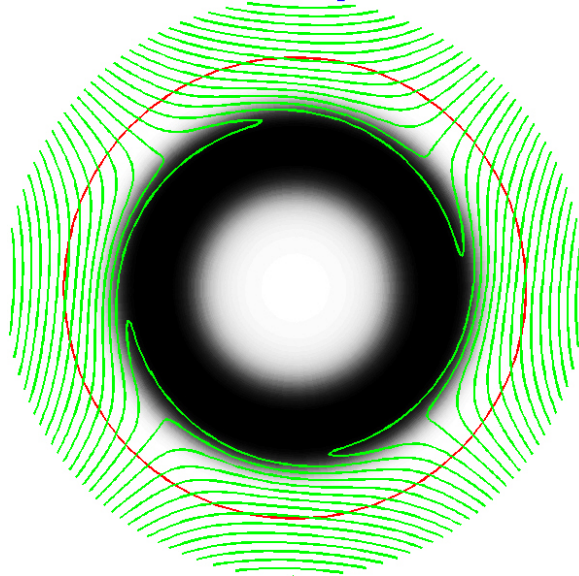
Quadrupole coil set: $\alpha = \pi/12$



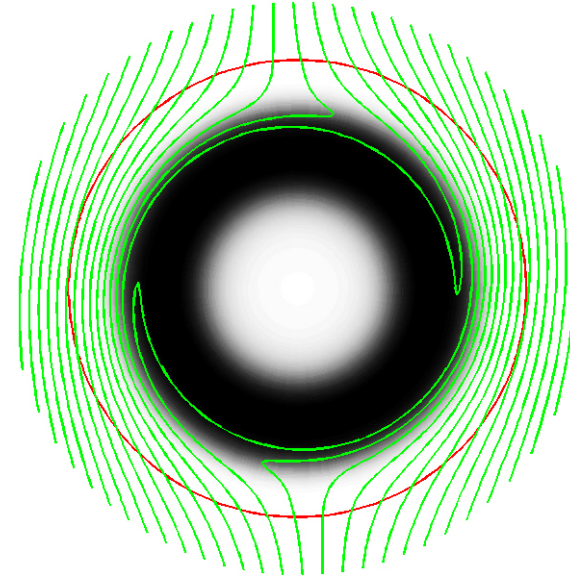
Potential advantage to quadrupole



Quadrupole



Dipole



- Symmetric radial and azimuthal force on plasma
- Quadrupoles are known to stabilize $n=2$ rotational modes, and should be effective at centering the plasma
- For a constant uniform resistivity, numerical calculations predict slightly better current drive for quadrupoles.
- Reduce turbulence and lower resistivity?

MHD Model



$$\frac{\partial n}{\partial t} + \nabla \cdot n \mathbf{u} = 0$$

$$Mn \left[\frac{\partial \mathbf{u}}{\partial t} + \mathbf{u} \cdot \nabla \mathbf{u} \right] = \frac{\mathbf{J} \times \mathbf{B}}{c} - \nabla P - \nabla \cdot \Pi$$

$$\frac{\partial \mathbf{A}}{\partial t} = \mathbf{u} \times \mathbf{B} - \eta c^2 \left(\frac{\mathbf{J}}{c} \right) - \frac{c}{en} \left[\left(\frac{\mathbf{J}}{c} \times \mathbf{B} \right) - \nabla P_e \right]$$

$$\frac{\partial S}{\partial t} + \nabla \cdot S \mathbf{u} = \frac{\gamma - 1}{n^{\gamma-1}} \left[\eta \mathbf{J}^2 + \nabla \cdot (k_{\perp} \nabla T) - \Pi : \nabla \mathbf{u} - R \right]$$

$$S = n^{2-\gamma} T$$

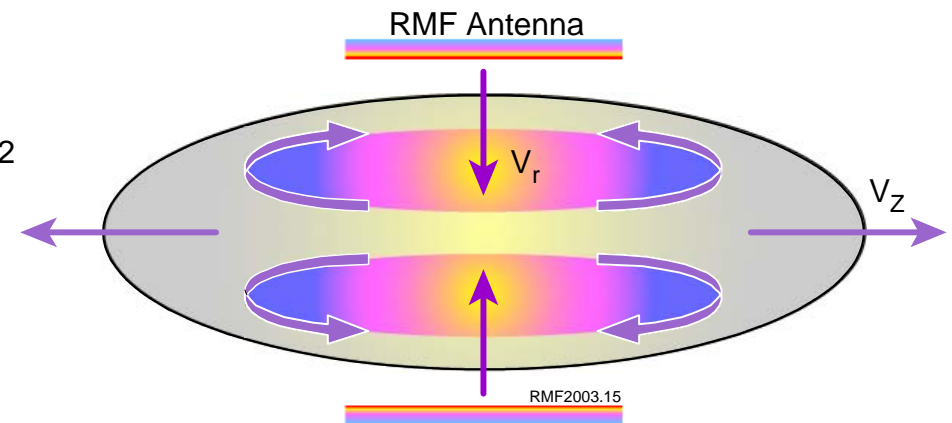
$$P = nk_B T$$

$$\mathbf{B} = \nabla \times \mathbf{A}$$

$$\mathbf{J} = \frac{c}{4\pi} \nabla \times \mathbf{B}$$

$$\Pi = -\frac{\mu}{Mn} \nabla \mathbf{u}$$

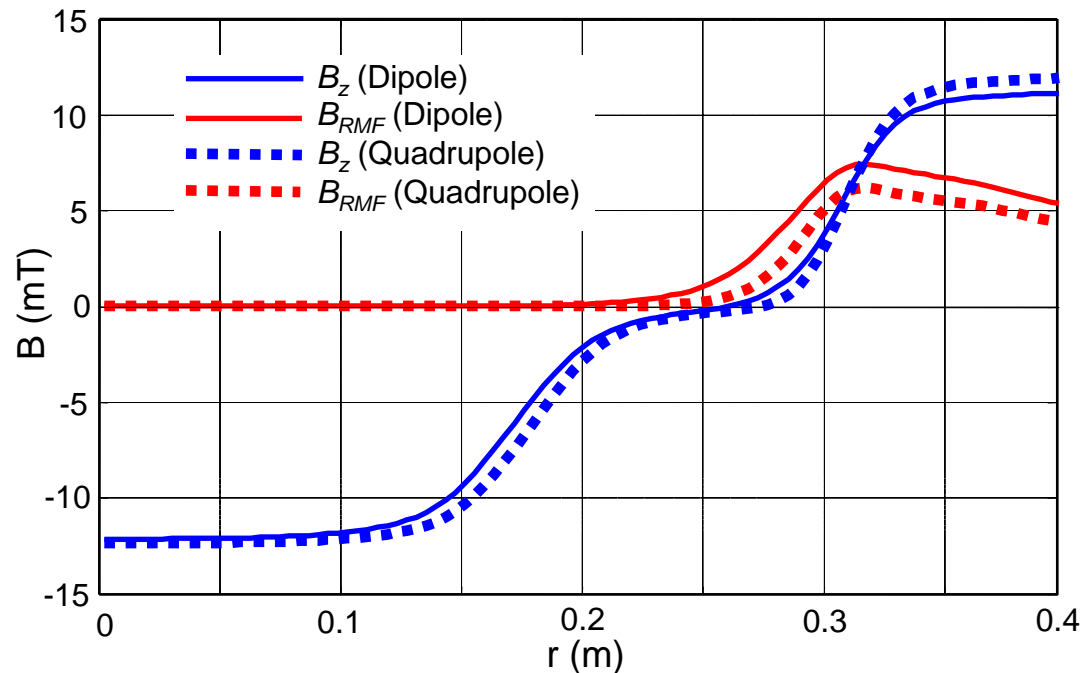
- Equations are solved numerically in the r- θ plane.
- To study FRC sustainment, two axial effects must be included:
 - Average β condition: $\langle \beta \rangle = 1 - \frac{1}{2} \chi_s^2$
 - Equalization of temperature and density (pressure) between inner and outer field lines (including effects of rotation).



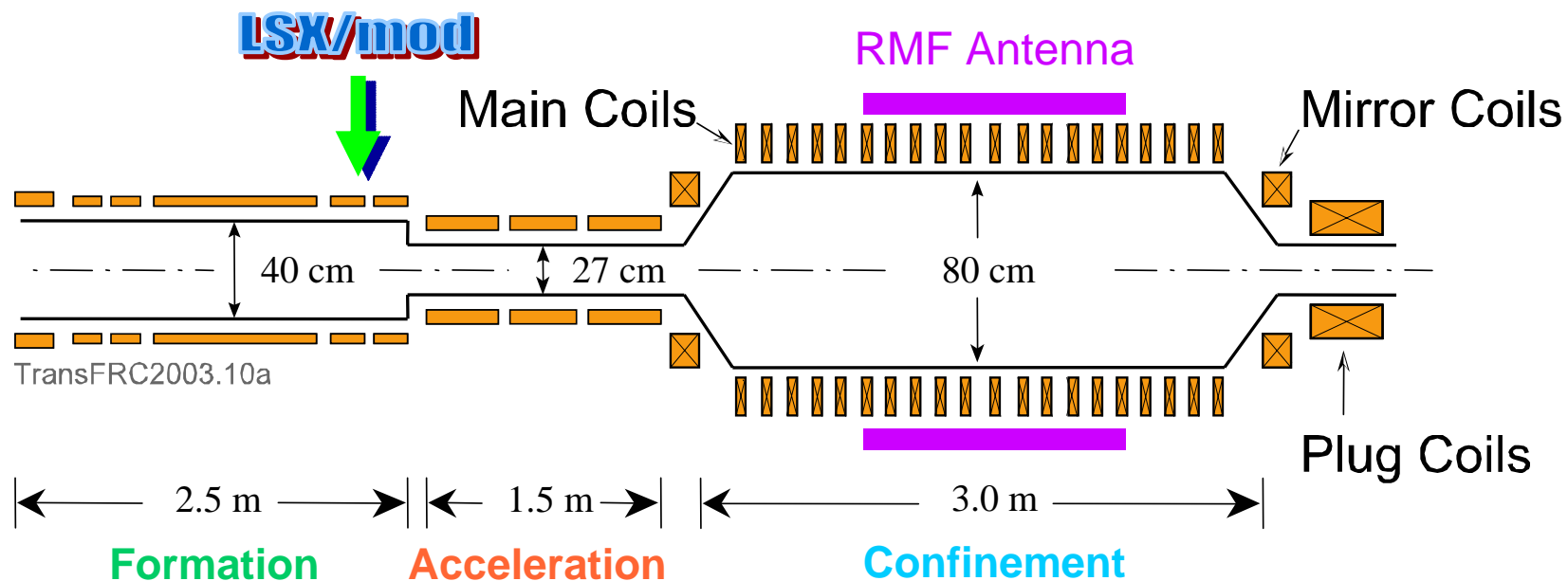
Numerical Predictions



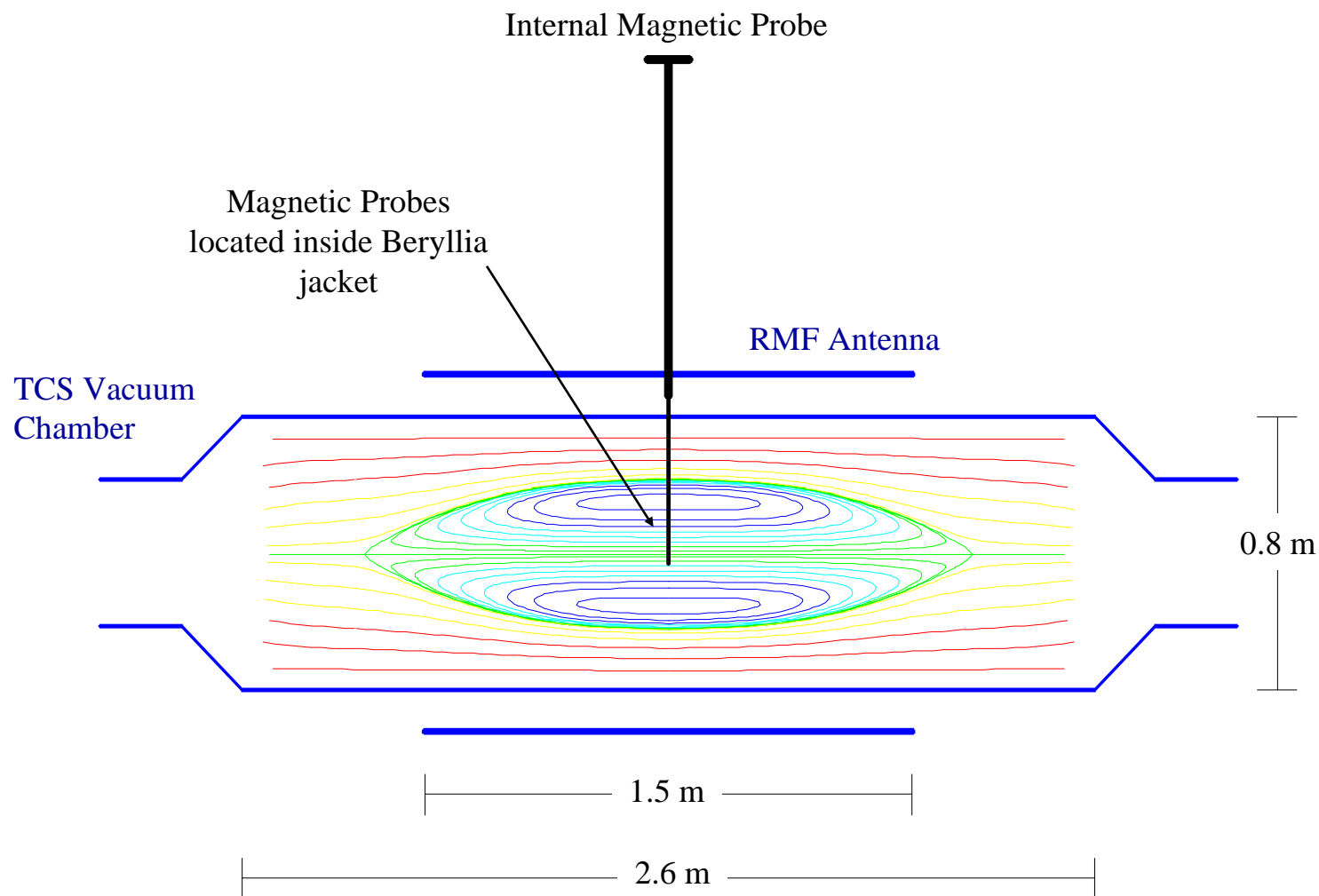
- Numerical simulations using RMF2 (a 2D (r - θ) Hall MHD code).
- Parameters similar to experimental parameters.
 - Uniform resistivity ($\eta = 100 \mu\Omega\text{-m}$)
 - $T_{total} = 30 \text{ eV}$, Vacuum $B_{RMF}(r = r_{wall}) = 3.5 \text{ mT}$
 - $f_{RMF} = 105 \text{ kHz}$ (Dipole), 210 kHz (Quadrupole)



The TCS Facility



The Internal Magnetic Probe



Signal Processing Internal Probe Data

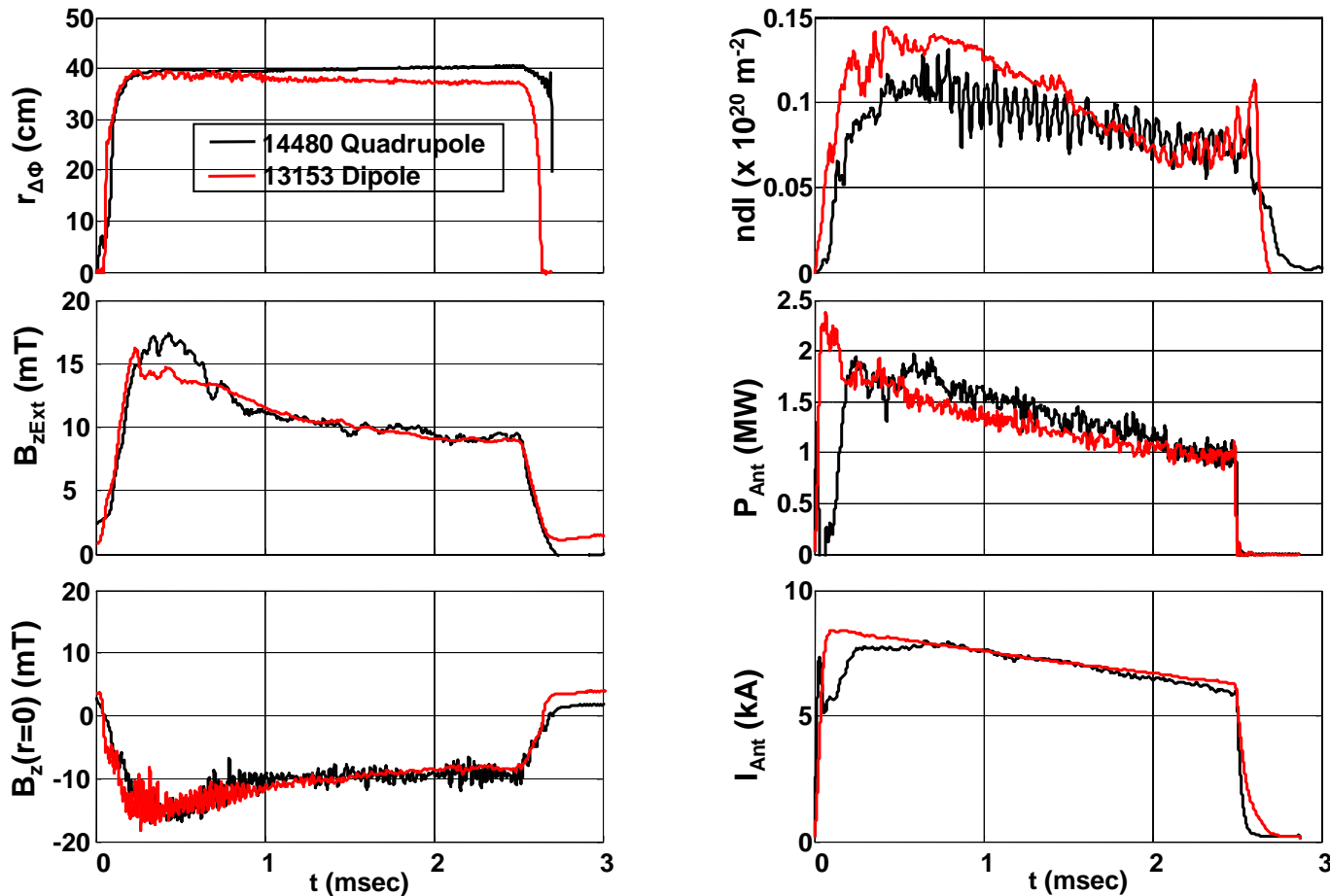


- Probe can be aligned to measure B_x only, B_z only, or at 45° to measure both B_x and B_z .
- With the probe at 45° , so that both B_x and B_z are measured, it is assumed that:
 - The signal within ± 10 kHz of f_{RMF} is RMF signal and is thus in the x-direction.
 - The rest is assumed to be in the z-direction.
 - This is not always a good assumption.

Experimental Results: Current Drive Efficiency



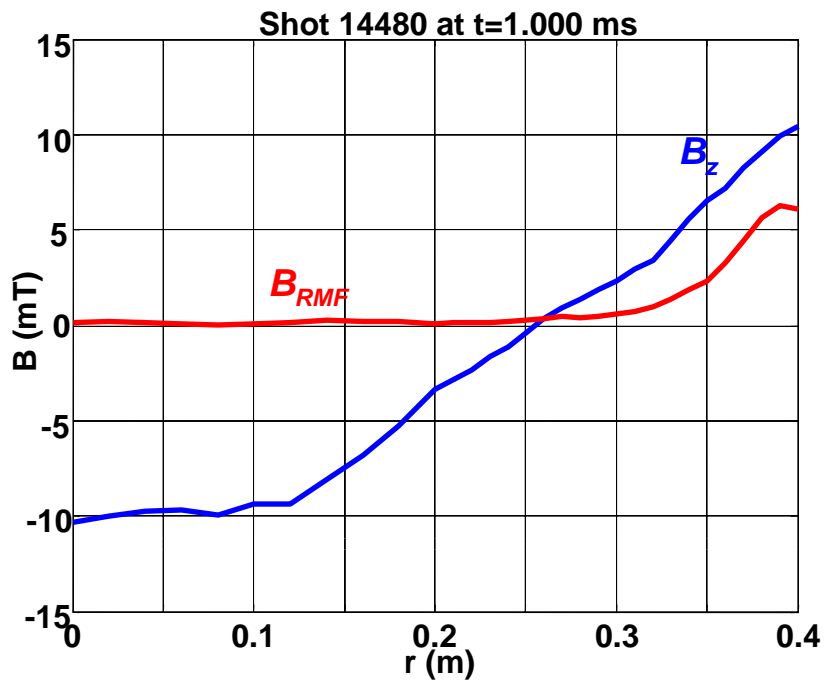
- Quadrupole RMF drives current as efficiently as Dipole RMF at given I_{Ant} and similar effective ω_{rmf} (105 kHz vs. 260 kHz)



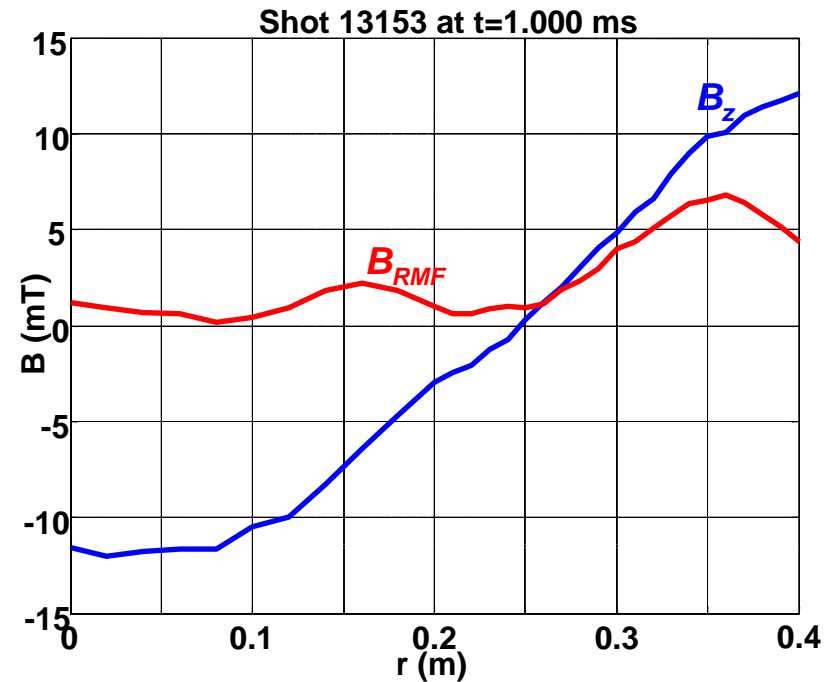
Internal Profiles



Quadrupole ($\omega=260$ kHz)

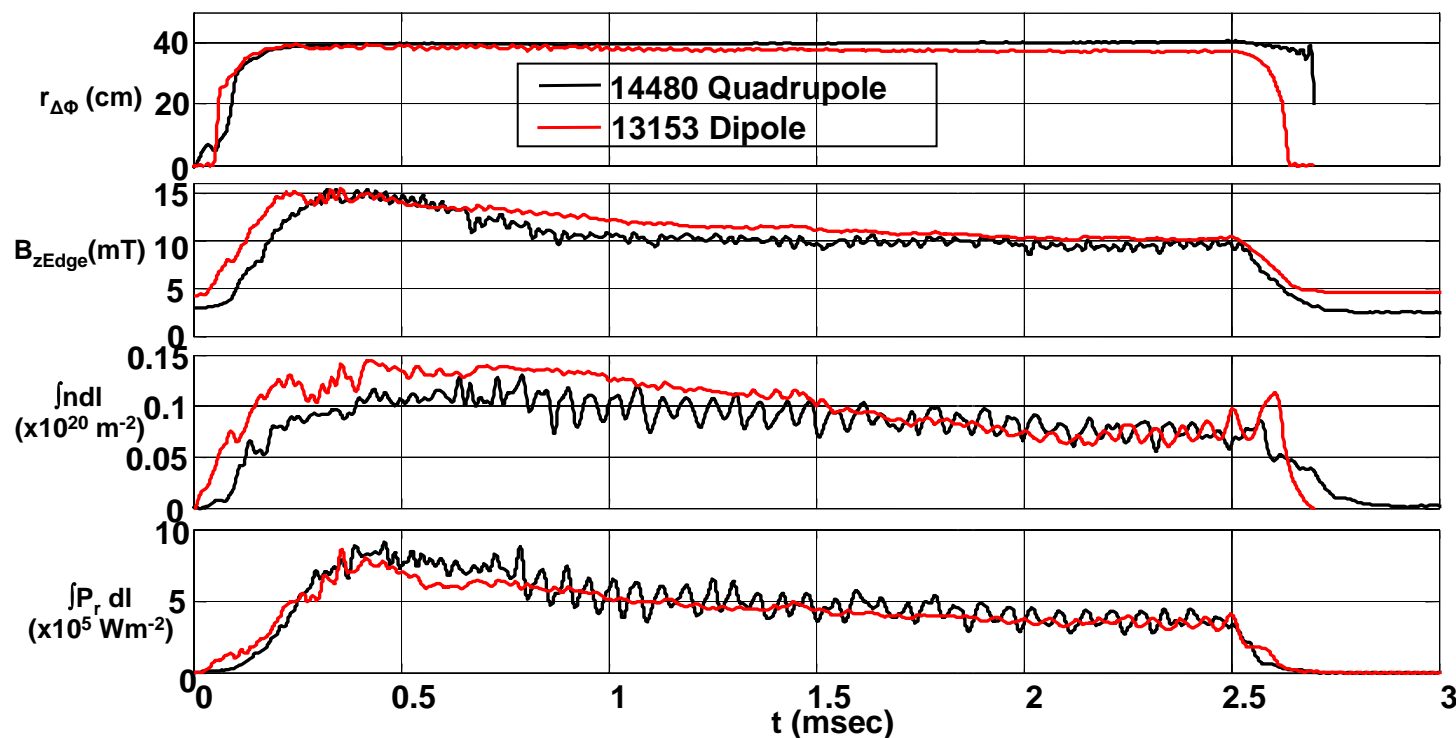


Dipole ($\omega=105$ kHz)



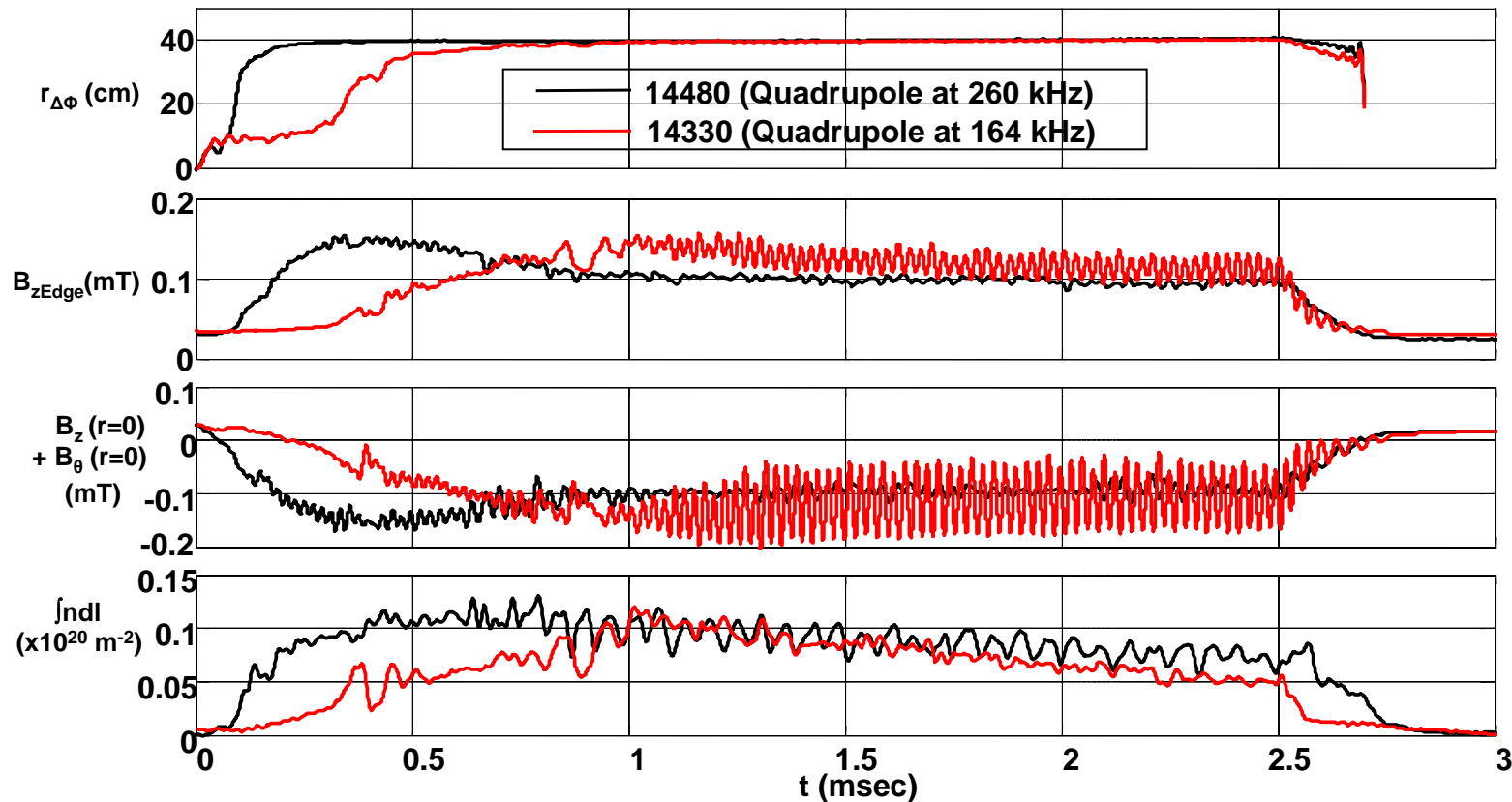
- However, quadrupole RMF is more localized at the edge.

More prone to n=2



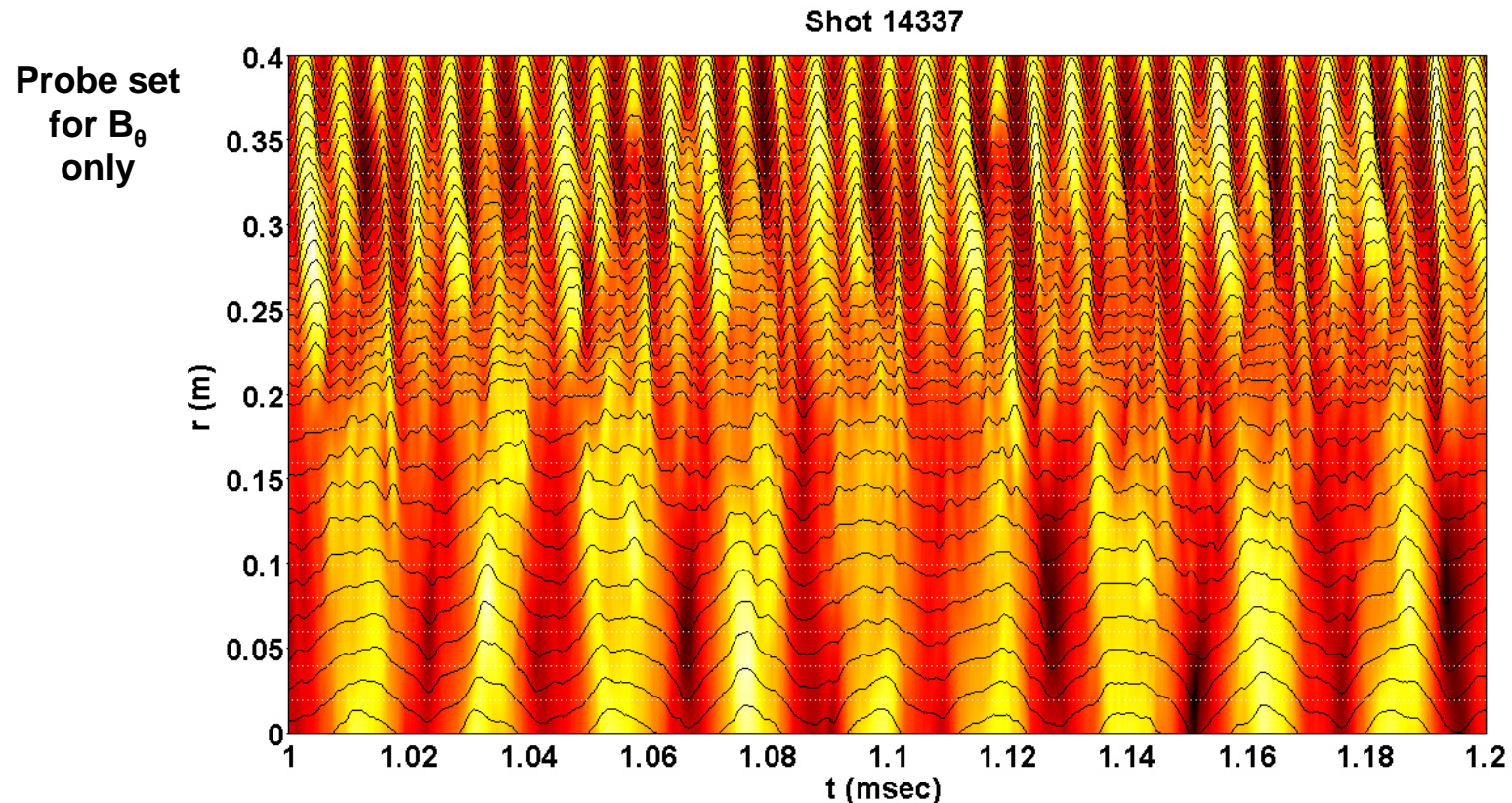
- As a result, FRCs formed by quadrupole RMF is more prone to n=2, possibly due to insufficient RMF present near field null where centrifugal force is strong (*H.Y. Guo et al, this meeting*).
- $f_{Rot} \sim 9$ kHz, similar to the dipole case.
- As in the dipole case, reducing ω aggravates rotational instabilities.

Stronger Internal Oscillations



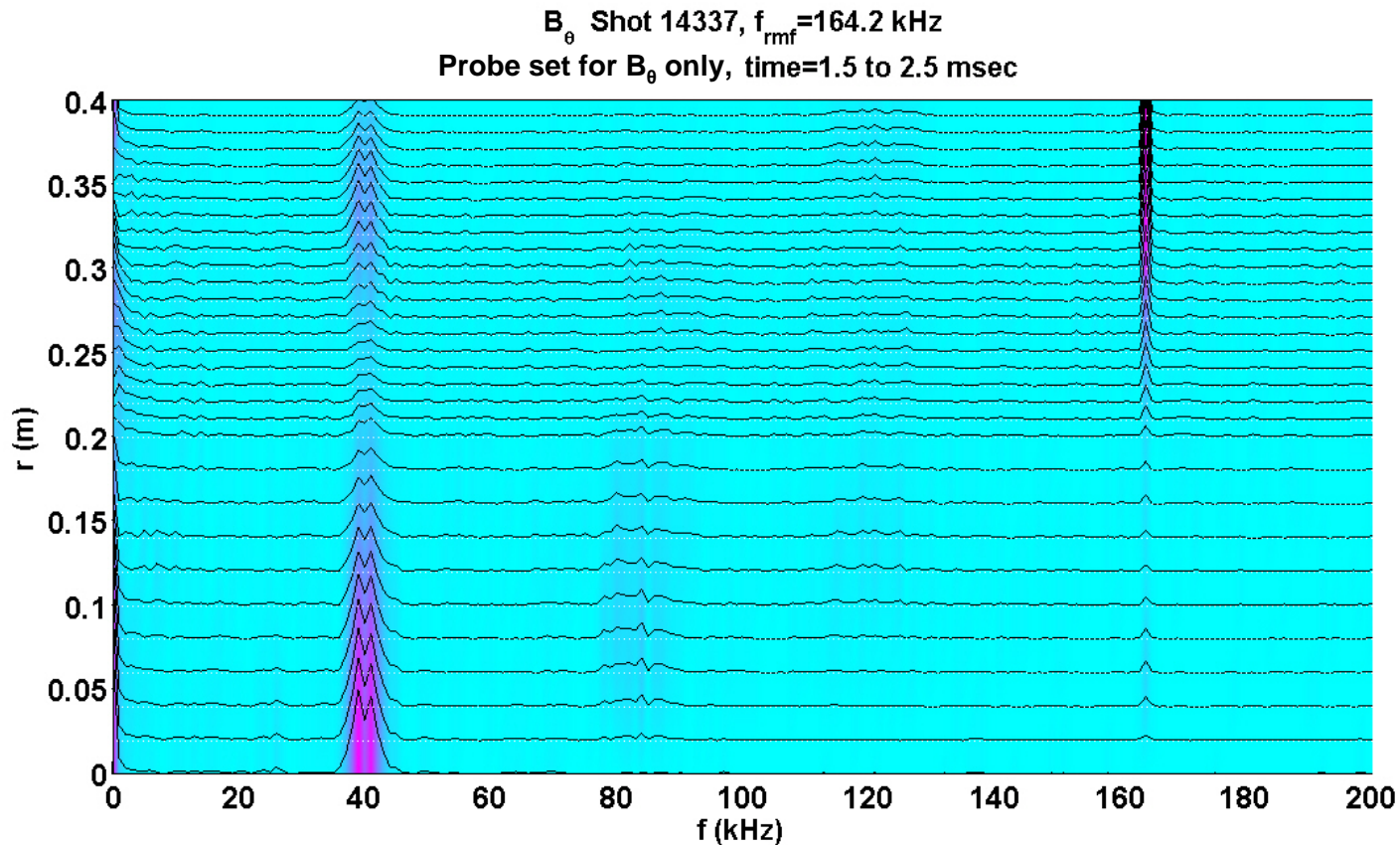
- Quadrupole RMF also leads to strong internal oscillations in B_θ , especially at lower ω , i.e., 164 kHz (#14330).
- Note that oscillations appear as r_s approaches the wall, and persist until the end of the pulse.

Internal oscillations in B_θ



- Quadrupole RMF driven FRCs tend to develop low frequency internal oscillations in B_θ , especially at large x_s and low RMF frequency.
 - Large amplitude (comparable to RMF amplitude at $r = r_{wall}$).
 - Penetrate to $r = 0$.

Internal oscillation spectrum



- The B_θ spectrum has a dominant low frequency spike.
 - Large amplitude at small and large radius.
 - $\sim 180^\circ$ phase shift between inner and outer regions

Inner mode structure

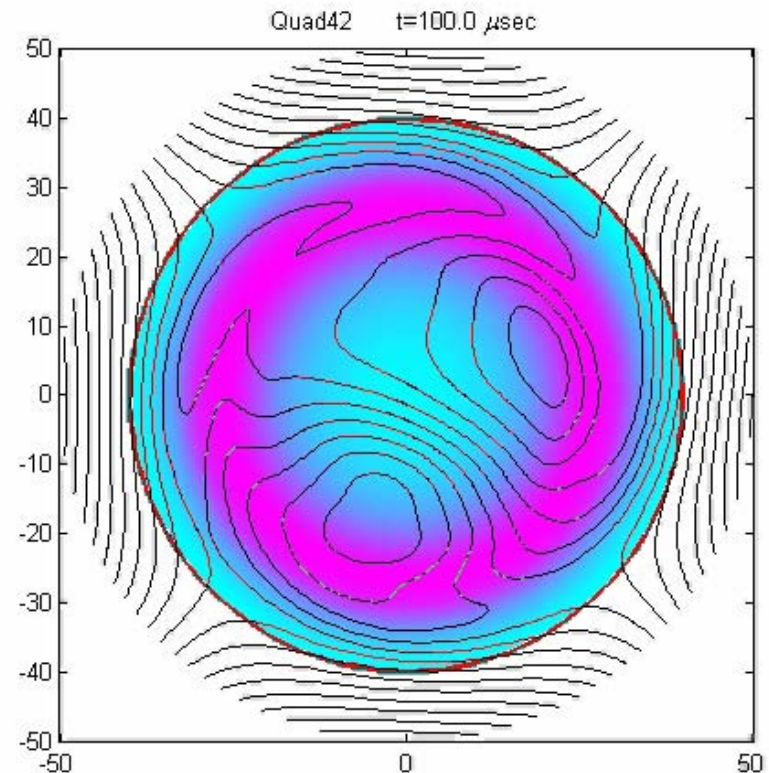


- Antennas produce a rotating $n=2$ field, which is confined to the outer region of the FRC.
- An internal $n=1$ field spontaneously develops, and fully penetrates the FRC (all the way to the null).
 - We believe that it is an $n=1$ field because:
 - It co-rotates with the electrons and produces a single cycle in the rotation time of the electron fluid. (The rotation frequency of the electron fluid can be calculated using the internal magnetic profile and the interferometer.)
 - It fully penetrates to $r = 0$ (higher order modes must vanish at the axis of symmetry)
- What is the source of the low frequency inner field?
 - Tilt ?

Numerical calculation with inner structure



- Numerical simulations using RMF2
 - a 2D (r - θ) Hall MHD code.
- Simulations do not spontaneously produce inner rotating structure.
- Simulations with an initial $n=1$ internal structure, and a resistivity profile that is sharply peaked near the edge yield signals similar to the experimental observations.
- Inner current is driven by the rotating internal structure.
- A torque is applied to the structure through the continuous tearing and reconnection of field lines (as in “*edge-driven mode*”).



Summary



- Quadrupole RMF is as efficient as dipole RMF for a given antenna current, and similar effective ω_{RMF} . (Quadrupole antennas must be driven at double the frequency.)
- Quadrupole RMF is more localized to the edge.
- FRCs driven by quadrupole RMF are more prone to the $n=2$ instability.
- FRCs driven by quadrupole RMF are prone to large internal oscillations.
- The above observations \rightarrow narrow operating range for quiescent, stable FRCs.